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СЕРИЯ

«МАТЕМАТИЧЕСКОЕ МОДЕЛИРОВАНИЕ И ПРОГРАММИРОВАНИЕ»

Решением ВАК России включен в Перечень рецензируемых научных изданий

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(национальный исследовательский университет)»**

Основной целью издания является пропаганда союза качественных и численных исследований математических моделей. Предпочтение при публикации будут иметь статьи, посвященные результатам качественных исследований математических моделей, выявляющих какие-либо неочевидные их свойства; результатам численных исследований, содержащих разработки новых вычислительных алгоритмов применительно к математическим моделям; и комплексам программ, созданным для постановки вычислительных экспериментов.

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Main purpose of the publication is to promote the union of the qualitative of numerical studies of mathematical models. Articles, devoted to the results of qualitative studies of mathematical models, that identify any non-obvious properties, the results of numerical studies that contain the development of new computational algorithms applied for the computational experiments, will have the preference for publication.

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